

# Dribbling Control of Omnidirectional Soccer Robots

Xiang Li, Maosen Wang and Andreas Zell

**Abstract**—This paper focuses on the dribbling control problem of an omnidirectional mobile robot. Because the movement of the dribbled object must be considered, dribbling control is more challenging than normal mobile robot motion control. A new feedback control algorithm, which steers a reference point to follow the desired movement and keeps the ball near to this point simultaneously, is proposed. To dribble a rolling ball along a given path, the robot should provide the ball with appropriate force by consecutive pushing operations when they travel in an environment with obstacles. Based on the analysis of the forces acting on the ball with respect to the mobile robot coordinate system, a constraint for robot movement in the dribbling process is also introduced. The simulation and real-world experiments address the performance of this control algorithm.

## I. INTRODUCTION

Dribbling control is a challenging task in the RoboCup Middle Size domain. As the rules only allow one third of the ball to be covered by the dribbler, the dribbling behavior has high requirements to the robot motion control. Some teams fulfill the dribbling task by planning robot moving paths [1] or designing the behavior-based approach [2], where the mobile robot is controlled towards the desired postures. The postures are generated by a planner based on the robot dynamic or kinematic model. However, how the robot can travel without losing the ball is not considered.

Considering the difficulty of determining the ball's motion when it is in continuous contacts with a robot, many RoboCup teams use neural networks ([3], [4]) and reinforcement learning methods ([5], [6], [7]) to learn some basic skills of the robot, such as kicking and dribbling. Although suitable simulation systems can support the learning before the experiments with a real robot, the skill learning needs long time and high computational cost.

In this paper we address the dribbling control problem for an omnidirectional robot. With the analysis of the force exerted on the ball inspired by [8], we obtain a constraint of robot movement in the dribbling process for keeping a rolling ball. Under this constraint, the task of dribbling a ball to follow a given path is completed by approaching a reference point to the given path and steering the ball to move around this point simultaneously.

## II. ROBOT KINEMATIC MODEL

The mobile robot used in this dribbling task is an omnidirectional robot, whose base is shown in Fig. 1. It has three Swedish wheels mounted symmetrically with 120 degrees

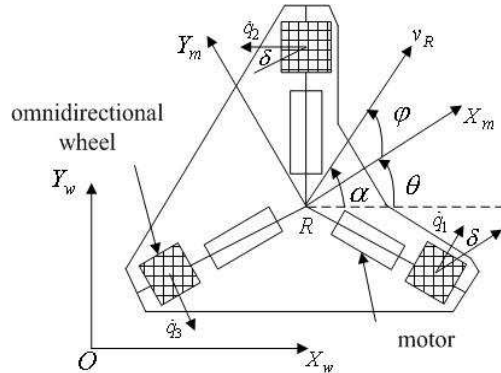


Fig. 1. Kinematics diagram of the base of an omnidirectional robot

from each other. Each wheel is driven by a DC motor and has a same distance  $L_w$  to the robot's center of mass  $R$ .

Besides the fixed world coordinate system  $[X_w, Y_w]$ , a mobile robot fixed frame  $[X_m, Y_m]$  is defined, which is parallel to the floor and whose origin locates at  $R$ .  $\theta$  denotes the robot orientation, which is the direction angle of the axis  $X_m$  in the world coordinate system.  $\alpha$  and  $\varphi$  denote the direction of the robot translation velocity  $v_R$  observed in the world and robot coordinate system, respectively. The kinematic model with respect to the robot coordinate system is given by :

$$\mathbf{v} = \begin{bmatrix} \sqrt{3}/3 & -\sqrt{3}/3 & 0 \\ 1/3 & 1/3 & -2/3 \\ 1/(3L_w) & 1/(3L_w) & 1/(3L_w) \end{bmatrix} \dot{\mathbf{q}}, \quad (1)$$

where  $\mathbf{v} = [\dot{x}_R^m \ \dot{y}_R^m \ \omega]^T$  is the vector of robot velocities observed in the robot coordinate system;  $\dot{x}_R^m$  and  $\dot{y}_R^m$  are the robot translation velocities;  $\omega$  is the robot rotation velocity.  $\dot{\mathbf{q}}$  is the vector of wheel velocities  $[\dot{q}_1 \ \dot{q}_2 \ \dot{q}_3]^T$ , and  $\dot{q}_i$  ( $i = 1, 2, 3$ ) is the  $i$ -th wheel velocity, which is equal to the wheel's radius multiplied by the wheel's angular velocity.

Introducing the transformation matrix from the robot coordinate system to the world coordinate system as

$${}^w R_m = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}, \quad (2)$$

the kinematic model with respect to the world coordinate system is deduced as:

$$\dot{\mathbf{x}} = \begin{bmatrix} \frac{2}{3} \cos(\theta + \delta) & -\frac{2}{3} \cos(\theta - \delta) & \frac{2}{3} \sin \theta \\ \frac{2}{3} \sin(\theta + \delta) & -\frac{2}{3} \sin(\theta - \delta) & -\frac{2}{3} \cos \theta \\ \frac{1}{3L_w} & \frac{1}{3L_w} & \frac{1}{3L_w} \end{bmatrix} \dot{\mathbf{q}}, \quad (3)$$

Xiang Li, Maosen Wang and Andreas Zell are with the Department of Computer Architecture, Wilhelm-Schickard-Institute, University of Tübingen, Sand 1, 72076 Tübingen, Germany {xiang.li, maosen.wang, andreas.zell}@uni-tuebingen.de



along the desired path and keeping the ball near to point  $E$  simultaneously, with the consideration of the decoupled translation and rotation of the omnidirectional robot. In the next sections, we present the path following control of point  $E$  based on its linearized kinematic equations and the ball keeping method with a PD controller.

### A. Linearizing Kinematic Model

As point  $E$  is taken as a fixed point  $(L,0)$  with respect to the robot coordinate system, its position can be transformed to the world coordinate system by

$$x_E = x_R + L \cos \theta \quad (9)$$

$$y_E = y_R + L \sin \theta, \quad (10)$$

where  $x_R$  and  $y_R$  denote the robot position in the world coordinate system;  $x_E$  and  $y_E$  denote the point  $E$ 's position in the world coordinate system.

By differentiating equations (9) and (10) with respect to time and introducing (4), we get the velocities of point  $E$  as

$$\dot{x}_E = \dot{x}_R^m \cos \theta - \dot{y}_R^m \sin \theta - L\omega \sin \theta \quad (11)$$

$$\dot{y}_E = \dot{x}_R^m \sin \theta + \dot{y}_R^m \cos \theta + L\omega \cos \theta, \quad (12)$$

where  $\dot{x}_R$  and  $\dot{y}_R$  are with respect to the world coordinate system.

Combining equations (11) and (12) with the robot rotation velocity, the kinematic model of point  $E$  is deduced as,

$$\dot{\mathbf{x}} = G\mathbf{v}, \quad (13)$$

where

$$\dot{\mathbf{x}} = [\dot{x}_E \ \dot{y}_E \ \dot{\theta}]^T,$$

$$G = \begin{bmatrix} \cos \theta & -\sin \theta & -L \sin \theta \\ \sin \theta & \cos \theta & L \cos \theta \\ 0 & 0 & 1 \end{bmatrix},$$

$$\dot{\mathbf{x}}_m = [\dot{x}_R^m \ \dot{y}_R^m \ \omega]^T.$$

Although this system is nonlinear because of the trigonometric functions of angle  $\theta$ , it can be linearized by inducing a simple compensator  $C = G^{-1}$ , because the matrix  $G$  is full rank. The linearized system  $\dot{\mathbf{x}} = \mathbf{u}$  is shown in Fig. 3 and has a new input vector  $\mathbf{u} = [u_1 \ u_2 \ u_3]^T$ .

This linear system is completely decoupled and allows the controlling of point  $E$  to follow any reference path and  $\theta$  to track any desired orientation in a separate way.

When a controller  $K$  is designed based on this simple linear system, the controller for the nonlinear system is generated as  $CK$ . The overall control loop, which consists of the nonlinear system, the compensator and the controller, is shown in Fig. 4.

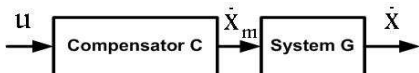


Fig. 3. Linearized system by the component  $C$

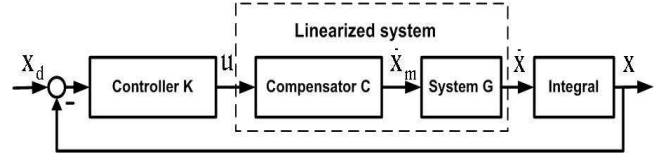


Fig. 4. Closed-loop control system

### B. Path Following Control of Point $E$

The path following problem is illustrated in Fig. 5.  $P$  denotes the given path. Point  $Q$  is the orthogonal projection of  $E$  on the path  $P$ .  $\mathbf{x}_t$  and  $\mathbf{x}_n$  are the tangent and normal unit vectors at  $Q$ , respectively. The path coordinate system  $x_t Q x_n$  moves along the path  $P$ .  $\theta_P$  is the path tangent direction at point  $Q$ .  $\theta_E$  denotes  $E$ 's moving direction. The angular error is defined as  $\tilde{\theta}_E = \theta_E - \theta_P$ .

Based on the above definitions, the path following problem is to find proper control values of  $E$ 's linear velocity  $v_E$  and angular velocity  $\dot{\theta}_E$  such that the deviation distance  $x_n$  and angular error  $\theta_E$  tend to zero.

To solve this path following problem, a Lyapunov candidate function

$$V = \frac{1}{2} K_d x_n^2 + \frac{1}{2} K_\theta \tilde{\theta}_E^2 \quad (14)$$

can be considered, where  $K_d$  and  $K_\theta$  are positive constants. The time derivation of  $V$  results in

$$\dot{V} = K_d x_n \dot{x}_n + K_\theta \tilde{\theta}_E \dot{\tilde{\theta}}_E. \quad (15)$$

A simple control law [9] is utilized here. It is only based on the deviation of point  $E$  to the given path, and controls point  $E$  moving along an exponential curve to converge to the axis  $x_t$ . The exponential curve is expressed as

$$x_n = x_{n_0} \exp(-kx_t), \quad (16)$$

where  $x_{n_0}$  is the deviation and the positive constant  $k$  determines the convergence speed of the deviation. Differentiating (16) with respect to  $x_t$ , we get the tangent direction of the exponential curve as

$$\tilde{\theta}_E = \arctan\left(\frac{dx_n}{dx_t}\right) = \arctan(-kx_n). \quad (17)$$

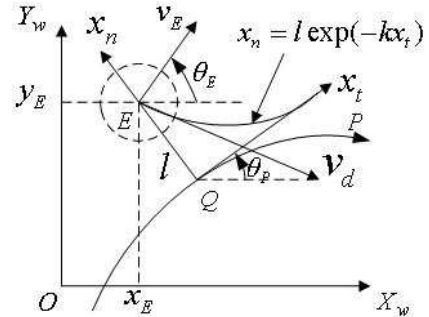


Fig. 5. Illustration of the path following problem

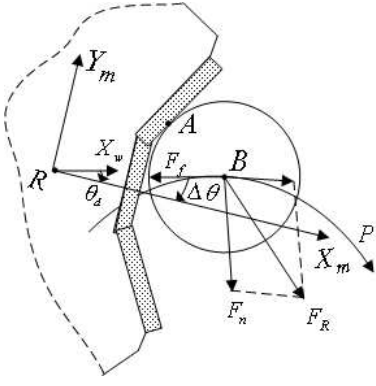


Fig. 6. Forces analysis for ball following a curve

Therefore, for a non-zero constant velocity  $v_d$ , the velocity of point  $E$  in the coordinate system  $x_t O x_n$  results in

$$\dot{x}_n = v_d \sin \tilde{\theta}_E, \quad (18)$$

$$\dot{x}_t = v_d \cos \tilde{\theta}_E. \quad (19)$$

Substituting the time derivative of  $\tilde{\theta}_E$  into (15), we get

$$\dot{V} = K_d x_n \dot{x}_n + k K_\theta \arctan(-kl) \frac{-\dot{x}_n}{x_n + (kx_n)^2} < 0, \quad (20)$$

because  $x_n \dot{x}_n = x_n v_d \sin(\arctan(-kx_n)) < 0$  and  $\dot{x}_n \arctan(kx_n) < 0$ . This solution of  $\dot{V}$  guarantees the global stability of the equilibrium at  $x_n = 0, \tilde{\theta}_E = 0$ , which means that this control law solves the path following problem.

Transforming the velocity of point  $E$  into the world coordinate system, we get the control values of the linear system as

$$u_1 = v_d \cos(\theta_E), \quad (21)$$

$$u_2 = v_d \sin(\theta_E), \quad (22)$$

where  $\theta_E = \tilde{\theta}_E + \theta_P$ .

The input of this controller is the relative distance between point  $E$  and the given path, which normally can be directly obtained by the sensors on the robot. Moreover, the deviation converges to zero smoothly with the speed controlled by parameter  $k$ , which can be chosen according to the performance requirement.

### C. Ball Keeping Control

As only two degrees of freedom are used to control point  $E$  to follow the given path, there is one remaining degree of freedom for the robot orientation which can be used for the ball keeping control. When a given path  $P$  performs a turning as shown in Fig. 6, the robot movement needs to be accurately controlled such that the force from the robot  $F_R$  is enough to overcome the friction  $F_f$  between the ball and the floor and provide the ball with sufficient centripetal force  $F_n$ . Although the shape of the robot's front can help the robot to exert the suitable force, it is necessary to keep the robot orientation having some deviation  $\Delta\theta$  to the tangent direction of the curve.

Based on the centripetal acceleration  $cv_d^2$ , we calculate the angle deviation as  $\Delta\theta = k_\theta cv_d^2$ , where  $k_\theta$  is the positive parameter. Then the ideal robot orientation  $\theta_d$  is given by

$$\theta_d = \theta_P + \Delta\theta, \quad (23)$$

A PD controller can be used to control the robot orientation to converge to the ideal one,

$$\omega = k_p(\theta_d - \theta) + k_d(\dot{\theta}_d - \dot{\theta}), \quad (24)$$

where  $\dot{\theta}_d$  and  $\dot{\theta}$  are the corresponding differential values of  $\theta_d$  and  $\theta$ ;  $k_p$  and  $k_d$  are the proportional and derivative gains, respectively.

Although a suitable dribbler mechanics can play a great role in providing friction for the robot keeping the ball, the robot movement should satisfy the condition given by (8). The required robot rotation velocity  $\omega$  must be constrained based on the required robot translation velocity coming from the path following control of point  $E$ . Since point  $E$  is considered as a fix point on the robot, the movement relationship between the robot and point  $E$  in vector notion is as follows:

$$\mathbf{v}_E = \mathbf{v}_R + \boldsymbol{\omega} \times \mathbf{r}_E^m, \quad (25)$$

$$\dot{\mathbf{v}}_E = \dot{\mathbf{v}}_R + \dot{\boldsymbol{\omega}} \times \mathbf{r}_E^m + \boldsymbol{\omega} \times \dot{\mathbf{r}}_E^m, \quad (26)$$

where  $\dot{\mathbf{v}}_E, \dot{\mathbf{v}}_R$  are the translation accelerations of point  $E$  and the robot with respect to the world coordinate system;  $\mathbf{r}_E^m$  is the position vector from  $R$  to  $E$  with respect to the robot coordinate system;  $\dot{\mathbf{r}}_E^m$  is the derivative of  $\mathbf{r}_E^m$ ;  $\dot{\boldsymbol{\omega}}$  is the robot rotation acceleration.

If point  $E$  is controlled with constant translation velocity moving along the given path, the tangent acceleration  $\mathbf{a}_t$  is equal to zero and the centripetal acceleration is  $cv_E^2$ . Substituting (26) into (7) and (8), the constraint of dribbling becomes

$$\mathbf{a}_t + cv_B^2 - \dot{\mathbf{v}}_E + \dot{\boldsymbol{\omega}} \times \mathbf{r}_E^m + \boldsymbol{\omega} \times \dot{\mathbf{r}}_E^m - (2\boldsymbol{\omega} \times \mathbf{v}_B^m + \dot{\boldsymbol{\omega}} \times \mathbf{r}_B^m + \boldsymbol{\omega} \times (\boldsymbol{\omega} \times \mathbf{r}_B^m)) < 0. \quad (27)$$

When the ball is near to point  $E$ ,  $\dot{\mathbf{r}}_E^m$  approximates to zero and  $\dot{\mathbf{r}}_B^m$  approximates to  $\dot{\mathbf{r}}_E^m$ . Then the above constraint can be reduced to

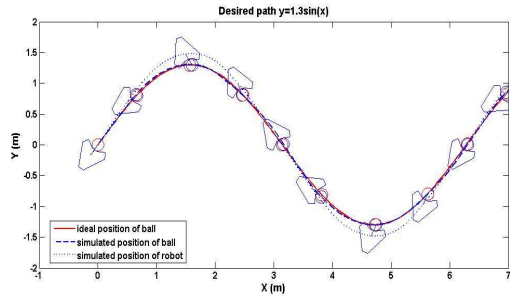
$$cv_B^2 - \dot{\mathbf{v}}_E - (2\boldsymbol{\omega} \times \mathbf{v}_B^m + \boldsymbol{\omega} \times (\boldsymbol{\omega} \times \mathbf{r}_B^m)) < 0. \quad (28)$$

## V. EXPERIMENTS

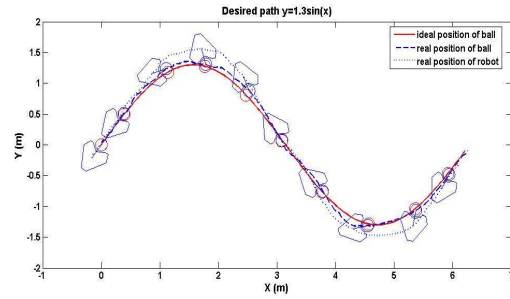
The control algorithm discussed above has been tested in both simulation and real-world environments, where the ball is required to follow a sinusoidal path  $y = 1.3 \sin x$  with constant translation velocity  $v_d = 1.2$  m/s.

### A. Simulation Experiment

In our simulator, the movements of the robot and the ball have been calculated from their kinematic equations. The pushing process is considered as a consecutive high frequency and low magnitude compact process. We utilize the basic collision equations, which describe the collisions of

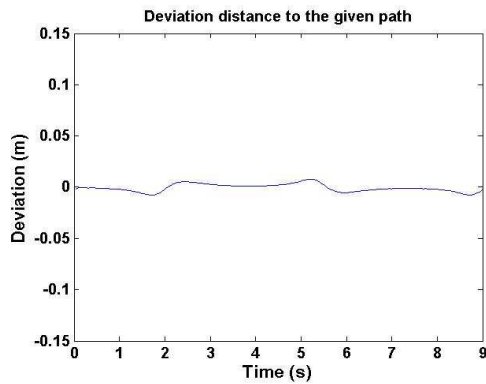


(a) Simulation

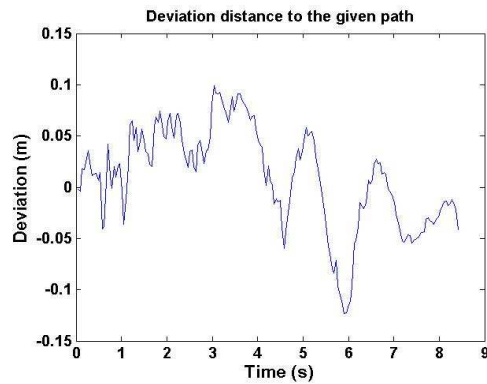


(b) Real-world experiment

Fig. 7. Ball follows the path  $y = 1.3 \sin x$  with  $v_d = 1.2$  m/s

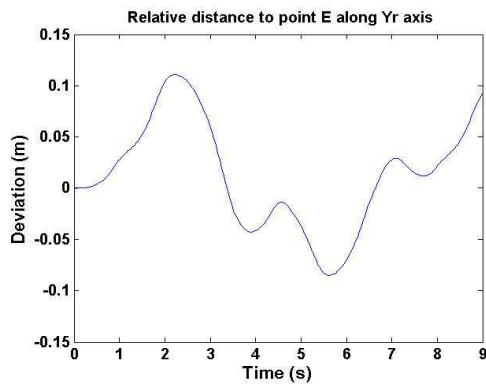


(a) Simulation

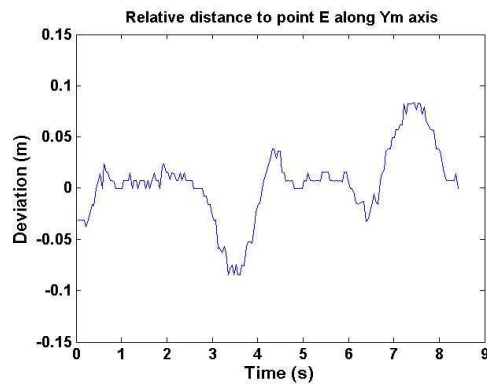


(b) Real-world experiment

Fig. 8. Deviation from point  $E$  to the desired path



(a) Simulation



(b) Real-world experiment

Fig. 9. Relative deviation from ball to point  $E$  along the axis  $Y_m$

two rigid bodies, and Newton's law of restitution to calculate the motion of the two objects after collisions.

The difficulty in this collision simulation is the exact determination of the collision moment. As a common method, we detect whether the robot and the ball overlap by some

degree due to the limited time; if they overlap, the simulation calculates  $n$  time steps backwards within the last cycle such that the overlap disappears. Since the simulation cycle is short enough, the accuracy of the collision detection is satisfiable. The parameters of our simulator, like the friction



Fig. 10. The real omnidirectional robot and ball

coefficient and the restitution coefficient, are adopted as experience values. The masses and the moment of inertia of robot and ball are adapted to the real values.

The parameters of our control algorithm were chosen as  $k = 3.5$ ,  $k_\theta = 0.9$ ,  $k_p = 10$ ,  $k_d = 6$ . These results illustrated in Fig. 7(a), 8(a) and 9(a) show us that the dribbling control method steers the point E converging to the given path with little deviation. Meanwhile, the ball does not slide away from the robot, because the ball's relative distance to point E along the axis  $Y_m$  is always less than the maximum value  $\pm 15\text{cm}$ .

### B. Real-world Experiment

The real-world experiment was made in our robot laboratory having a half-field of the RoboCup middle-size league. The ball's observation values come from our omnidirectional viewing system and object detection process. Our omnidirectional viewing system consists of a AVT Marlin F-046C color camera with a resolution of  $780 \times 580$ , which outputs images up 50 times per second. In order to achieve a complete surrounding map of the robot, the camera is assembled pointing up towards a hyperbolic mirror, which is mounted on the top of our omnidirectional robot, as shown in Fig. 10. After obtaining the image from the camera, a fast object detection algorithm is used to get the ball's real world position, as described in [10].

The parameters of our control algorithm were chosen as  $k = 3.5$ ,  $k_\theta = 0.9$ ,  $k_p = 5$ ,  $k_d = 3$ . Although measurement noise, environment disturbance and the actuator delay of the robot were induced, the experiment results illustrated in Fig. 7(b), 8(b) and 9(b) demonstrate that the control method has good performance.

## VI. CONCLUSIONS

In this paper a new control method for an omnidirectional robot dribbling a rolling ball is presented. This approach solves the control problem of the consecutive mobile robot pushing operation by introducing a reference point as the controlled object, which is also regarded as a fixed point of the robot itself. Feedback control methods are used to steer the reference point to follow the given path and the ball to move around the reference point simultaneously. In order to keep the ball, the relative movement between the robot and the ball has been analyzed and a constraint of

robot movement is presented, with which controller outputs, namely the required translation and rotation velocities, have been limited. With the Lyapunov stability theory, the global stability of the path following control law has also been proven.

The simulation and real-world experiments used a sinusoidal curve as the ideal path, and required a constant translation velocity of the ball. The results show that this control method can control the omnidirectional robot to apply appropriate pushing operations such that the ball follows the given path and does not slide away from the robot.

## VII. ACKNOWLEDGMENT

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